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Published in:

I E E E Transactions on Power Electronics

Link to article, DOI:

[10.1109/TPEL.2016.2549015](https://doi.org/10.1109/TPEL.2016.2549015)

Publication date:

2017

Document Version

Peer reviewed version

[Link back to DTU Orbit](#)

Citation (APA):

Mira Albert, M. D. C., Zhang, Z., Knott, A., & Andersen, M. A. E. (2017). Analysis, Design, Modeling, and Control of an Interleaved-Boost Full-Bridge Three-Port Converter for Hybrid Renewable Energy Systems. *I E E E Transactions on Power Electronics*, 32(2), 1138 - 1155. <https://doi.org/10.1109/TPEL.2016.2549015>

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Analysis, Design, Modelling and Control of an Interleaved-Boost Full-Bridge Three-Port Converter for Hybrid Renewable Energy Systems

Maria C. Mira, *Member, IEEE*, Zhe Zhang, *Member, IEEE*, Arnold Knott, *Member, IEEE*, Michael A. E. Andersen, *Member, IEEE*

Abstract—This paper presents the design, modelling and control of a three-port (TPC) isolated dc-dc converter based on interleaved-boost-full-bridge with pulse-width-modulation and phase-shift control for hybrid renewable energy systems. In the proposed topology, the switches are driven by phase-shifted PWM signals, where both phase angle and duty cycle are controlled variables. The power flow between the two inputs is controlled through the duty cycle, whereas the output voltage can be regulated effectively through the phase-shift. The primary side MOSFETs can achieve zero-voltage switching (ZVS) operation without additional circuitry. Additionally, due to the ac output inductor, the secondary side diodes can operate under zero-current switching (ZCS) conditions. In this work, the operation principles of the converter are analyzed and the critical design considerations are discussed. The dynamic behavior of the proposed ac inductor based TPC is investigated by performing state-space modelling. Moreover, the derived mathematical models are validated by simulation and measurements. In order to verify the validity of the theoretical analysis, design and power decoupling control scheme, a prototype is constructed and tested under the various modes, depending on the availability of the renewable energy source and the load consumption. The experimental results show that the two decoupled control variables achieve effective regulation of the power flow among the three ports.

Index Terms—Three-port converter, state-space modelling, renewable energy, energy storage, phase-shift and duty cycle control.

I. INTRODUCTION

THE application of clean and renewable energy, such as solar, wind and hydrogen, has been a focus in academia

and industry over the last decade [1], [2], [3]. Due to the intermittent feature of renewable energy sources, energy storage units are needed in order to balance the electricity generation and consumption within a power system having a high renewable energy penetration. Moreover, multiple energy sources hybridization can distinctly improve various aspects of system performance, such as decreasing cost, isolating energy sources from load fluctuations and enhancing the system dynamics. Hence, hybrid energy conversion systems are well suited for applications in which the average power demand is low whereas the load dynamics are relatively high [4], [5]. As a result, merging the renewable energy source elements together as a hybrid power conversion system, as well as controlling the power flows effectively has become a topic of interest.

In order to fulfil different system requirements, various hybrid system configurations and converter topologies have been proposed and investigated as reviewed in [3]. In applications where galvanic isolation is required, there are basically two categories classified as: multiple-converter conversion and multiple-port conversion. In the multiple-converter configurations, power converters are connected in parallel or in series in order to couple the energy sources and loads. By contrast, multiple-port power conversion systems can have high power density and low cost, due to the fact that some components and circuits in various power ports, such as transformers, rectifiers and output filters, can be shared as a common part along the power conversion path. Therefore, multiple-port converters have been receiving increased attention in recent years [6], [7], [8]. A general solution to obtain an isolated multiple-port converter is to adopt the magnetic coupling method, where various input power sources can be coupled with transformer windings or independent transformers [9], [10], [11]. In this solution, the multiport converter can be constructed from the basic high frequency switching cells, including the half-bridge (HB), full-bridge (FB), boost-half-bridge (BHB) and their combinations, according to the system constraints imposed by the features of the input power sources. Based upon this principle, a number of three-port (TPC) bidirectional dc-dc converters, which can

Manuscript received November 26, 2015; revised January 4, 2016; accepted March 15, 2016. Date of publication MONTH DAY, 2016; date of current version MONTH DAY, 2016

Recommended for publication by Associate Editor ADD.

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Color versions of one or more of the figures in this paper are available online at <http://ieeexplore.ieee.org>.

Digital Object Identifier ADD

fully isolate the various power ports and control the power flows into/out of each port, were reported in [12], [13], [14], [15], [16]. However, a large number of power switches have to be employed in those converters, resulting in increased cost and size. Besides the fully isolated multi-port topologies, partially isolated multiple-input converters, i.e. only some of the input/output ports are fully isolated, have been attracting more attention due to simple structure, less components and easy control. A dual-input dc-dc converter with BHB and FB switching cells was proposed in [17]. Two independent transformers are adopted in order to integrate both voltage-fed and current-fed power sources effectively. By combining a BHB with an LLC resonant tank, a wide-gain unidirectional two-port resonant converter is presented in [18], which can be extended to a TPC by replacing the low voltage dc bus with a voltage source. However, the control scheme to decouple the power flow will be complex due to the characteristics of the LLC circuitry. A systematic method for deriving a TPC with a diode rectifier was studied in [19], where the magnetizing inductance of an isolation transformer is utilized as a power interfacing element between the two non-isolated sources; however, this solution limits the converter's output power capability. A TPC based on an improved flyback-forward topology, with duty cycle and phase-shift control, proposed in [20], makes use of the leakage inductance of two coupled inductors to transfer power to the output port. However, in this solution the power delivering capability from the battery port to the output load is limited due to the flyback operation. Two three-port converter (TPC) topologies were proposed in [21] and [22] by integrating a boost converter into a phase-shift full-bridge buck converter, hence, the two non-isolated input ports, which connect with the renewable energy sources, are isolated from the load. After that, the topologies and their derived structures are investigated and presented in [23], [24], [25], [26]. By adopting the phase-shift with duty cycle control, the decoupled power flow can be controlled effectively among the various ports in a certain operating range. However, due to the employed output dc inductor, all the output rectifier diodes operate under hard switching condition, and suffer from high voltage stress and reverse recovery losses. Moreover, like other phase-shift zero-voltage switching (ZVS) converters, the duty cycle loss issue due to the leakage inductance still occurs. A FB TPC with duty cycle and phase-shift control derived from an interleaved boost-full-bridge (BFB) and a bridgeless boost rectifier is presented in [27]. This topology reduces the input current ripple and current stress of the input ports because of the 180° phase-shift operation of the primary switching legs. The output port regulation is achieved through the phase-shift between the primary and secondary switches. Therefore, two extra active switches in the secondary side are necessary to control the output port power flow, both with high side driver requirements, which increases the circuit complexity. Moreover, the body diode of the secondary MOSFETs operate under hard switched current conditions generating reverse recovery losses.

The goal of this work is to propose, analyse and design a TPC topology for hybrid renewable energy systems. The

proposed topology, as illustrated in Fig. 1, is derived from a ZVS HB inductive dc-dc converter with an active clamped circuit [28], [29]. By replacing the clamp capacitor in the ZVS circuit with the second voltage source, an additional input port can be obtained. Compared to the topologies in [21] and [25], the rectifier diodes achieve zero-current switching (ZCS) at turn-off avoiding reverse recovery losses. Additionally, the voltage across the diodes is inherently clamped by the output capacitor C_O , therefore, voltage rings caused by the stray inductance can be eliminated. Furthermore, the secondary freewheeling current is limited due to the absence of a dc output inductor. Moreover, this converter is superior to its LLC counterparts due to lower complexity of the modulation and control. Compared to previous research on TPC topologies, modelling and analysis of dynamic performance with multiple control parameters are seldom reported. The major contribution of this paper is to analyse the relation between the two control variables, phase-shift and duty cycle, and the system dynamics based on the converter small-signal model. The derived mathematical model is verified by simulations as well as experimental measurements. Based on the small-signal model, the power flow control is designed and the converter is tested under various operation modes, i.e. dual input (DI) mode, dual output (DO) mode and single input single output (SISO) mode.

This paper is organized into seven sections: following the introduction in Section I, the topology and operation principle of the proposed converter are presented in Section II. Design considerations and the associated guidelines are given in Section III. The dynamic behaviour is investigated in Section IV. The power flow regulation scheme is analysed in Section V. The corresponding experimental results from a laboratory prototype are provided and discussed in Section VI. As a final point, the conclusion is presented in Section VII.

II. CIRCUIT DESCRIPTION AND OPERATION PRINCIPLES

The studied topology in Fig. 1 consists of two input inductors, L_1 and L_2 , an ac inductor L_{ac} , four power MOSFETs $M_1 \sim M_4$, and a high frequency transformer with a turn ratio of 1: n . The ac inductor, which is the sum of the leakage inductance and the auxiliary inductance, is the power interface element between primary and secondary sides of the transformer. Switches M_1 , M_2 and M_3 , M_4 are driven with complementary gate signals with a deadband. V_1 and V_2 represent the input voltages; i_{L1} and i_{L2} are defined as the input inductor currents;

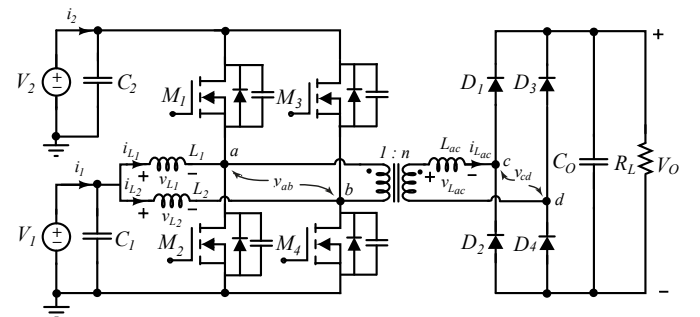


Fig. 1. Topology of the proposed TPC for hybrid renewable energy systems.

v_{ab} is the voltage between the midpoints of the bidirectional interleaved boost switching legs, and i_{Lac} is the current of the secondary side winding. In order to decouple the two inputs, V_1 and V_2 , and regulate the output voltage accurately, both the duty cycle and the phase-shift angle are adopted as the control variables simultaneously. The duty cycle of the power switches is used to adjust the power among the two independent sources, and the phase-shift angle between the midpoints of the full bridge is employed to regulate the power flow to the output port.

Through the phase-shift with duty cycle control, and according to the availability of the renewable energy source and the load demand, the proposed converter can operate in various operating modes: in DI mode when the load demand is higher than the available power from the renewable energy source and the energy storage element delivers the extra energy to the load; in DO mode when the input power is higher than the load power demand and the energy storage element balances the power by storing the excess energy; and in SISO mode when power transfers between the two inputs or from one of the inputs to the output port.

For the theoretical analysis it is assumed that inductors L_1 , L_2 and capacitors C_1 , C_2 , and C_0 are big enough and the deadband effect is negligible. Due to the operation symmetry, the variation range of the phase-shift angle φ is: $0 < \varphi < \pi$. Depending on the duty cycle and its relationship with the phase-shift angle, there are three operational cases existing, based on the current shape of the ac inductor, which can be classified as completely demagnetized, partially magnetized and fully magnetized.

Fig. 2 and Fig. 3 shows the equivalent circuits during the defined time intervals and the key operating waveforms when the ac inductor current is completely demagnetized in each period. During the first subinterval, i.e. $[0 \sim t_1]$ as shown in Fig. 2 (a), M_2 and M_3 are conducting simultaneously, so that L_1 and L_2 are charged and discharged, respectively. The voltage across midpoints a and b is clamped at $-V_2$, therefore, L_{ac} is charged with $(nV_{ab} - V_{cd})$. The ac inductor current is negative, as denoted in Fig. 2 (a), and satisfies

$$I_{Lacpk} = \frac{-nV_2 + V_o}{L_{ac}} \cdot \Phi T \quad (1)$$

where the phase-shift angle normalized to the period is defined as

$$\Phi = \frac{\varphi}{2\pi} \quad (2)$$

During the interval $[t_1 \sim t_2]$ in Fig 2 (b), M_4 is triggered at t_1 and L_1 and L_2 are charged. Since in this interval the voltage across the transformer, v_{ab} is clamped at zero, L_{ac} is discharged with a slope determined by the output voltage V_o . Defining β as the interval $[t_1 \sim t_2]$ normalized to the period as in (3), the ac inductor discharge interval Δt can be calculated as shown in (4).

$$\beta = \frac{nV_2 - V_o}{V_o} \cdot \Phi \quad (3)$$

$$\Delta t = t_2 - t_1 = \beta \cdot T \quad (4)$$

When the ac inductor current reaches zero the bridge rectifier diodes stop conducting, which concludes the second subinterval.

During subinterval $[t_2 \sim t_3]$, L_1 and L_2 will continue being charged, as represented in Fig. 2 (c), until M_2 is turned-off at t_3 . Since the ac inductor current is completely demagnetized during the previous interval, in this state there is no power transferring from the primary side to the output port.

The equivalent circuit during interval $[t_3 \sim t_4]$ is presented in Fig. 2 (d). It can be seen that the operation principle is symmetrical to that of $[0 \sim t_1]$, thus

$$I_{Lac}(t_4) = -I_{Lac}(t_1) \quad (5)$$

From the key waveforms shown in Fig. 3, it can be observed the phase-shift value, Φ , should be smaller than the duty cycle (D) and the complement of the duty cycle ($1 - D$), as expressed in (6).

$$\Phi < \min[D, (1 - D)] \quad (6)$$

Using equations (1) to (4), the output voltage of the converter can be obtained as in (7).

$$V_o = \frac{nV_2}{k} \cdot \Phi \left(-\Phi + \sqrt{\Phi^2 + 2k} \right) \quad (7)$$

where the parameter k is a dimensionless magnitude defined by the inductance, the output load and switching frequency as shown in (8).

$$k = \frac{2L_{ac}}{R_L T} \quad (8)$$

The relationship between V_1 and V_2 is obtained as

$$V_2 = \frac{V_1}{(1 - D)} \quad (9)$$

It is noteworthy that in this operation mode the energy transferred to the output port does not directly depend on the duty cycle. Therefore, in the completely demagnetized operating mode the power flow from V_1 and V_2 to the output port will be entirely controlled by Φ .

If the inductor current i_{Lac} does not decrease to zero before M_2 is triggered, the ac current is partially magnetized, as shown in Fig. 4 (a). The boundary condition between completely demagnetized and partially magnetized inductor current can then be derived as

$$\Delta t + \Phi T \leq (1 - D)T \quad (10)$$

Substitution of (4) into (10) leads to (11).

$$\Phi \leq \frac{(1 - D)}{M} \quad (11)$$

where the relation between the input and output ports is defined as

$$M = \frac{nV_{ab}}{V_{cd}} = \frac{nV_1}{(1 - D)V_o} = \frac{nV_2}{V_o} \quad (12)$$

In the same way, if the i_{Lac} does not reach zero before M_2 is turned off, the ac current becomes fully magnetized, as shown in Fig. 4 (b). As it can be observed from the inductor current shape in the key waveforms shown in Fig. 4, these operation modes, i.e. partial and fully magnetized, allow to transfer higher power to the output than the completely demagnetized counterpart. However, during the time intervals in which the inductor current does not reach zero, $[0 \sim t_1]$ in the partially magnetized mode and $[0 \sim t_1]$ and $[t_3 \sim t_4]$ in the fully

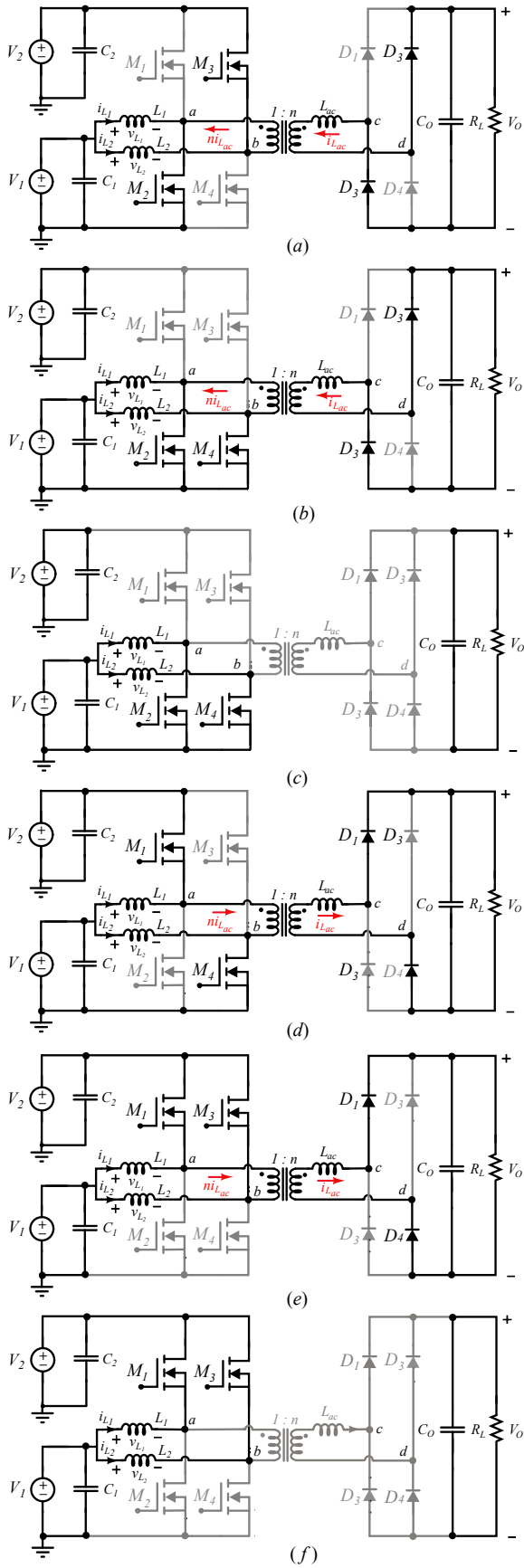


Fig. 2. Equivalent operating circuits for completely demagnetized output inductor current (left): (a) time interval $[0 \sim t_1]$, (b) time interval $[t_1 \sim t_2]$, (c) time interval $[t_2 \sim t_3]$, (d) time interval $[t_3 \sim t_4]$, (e) time interval $[t_4 \sim t_5]$ and (f) time interval $[t_5 \sim t_6]$.

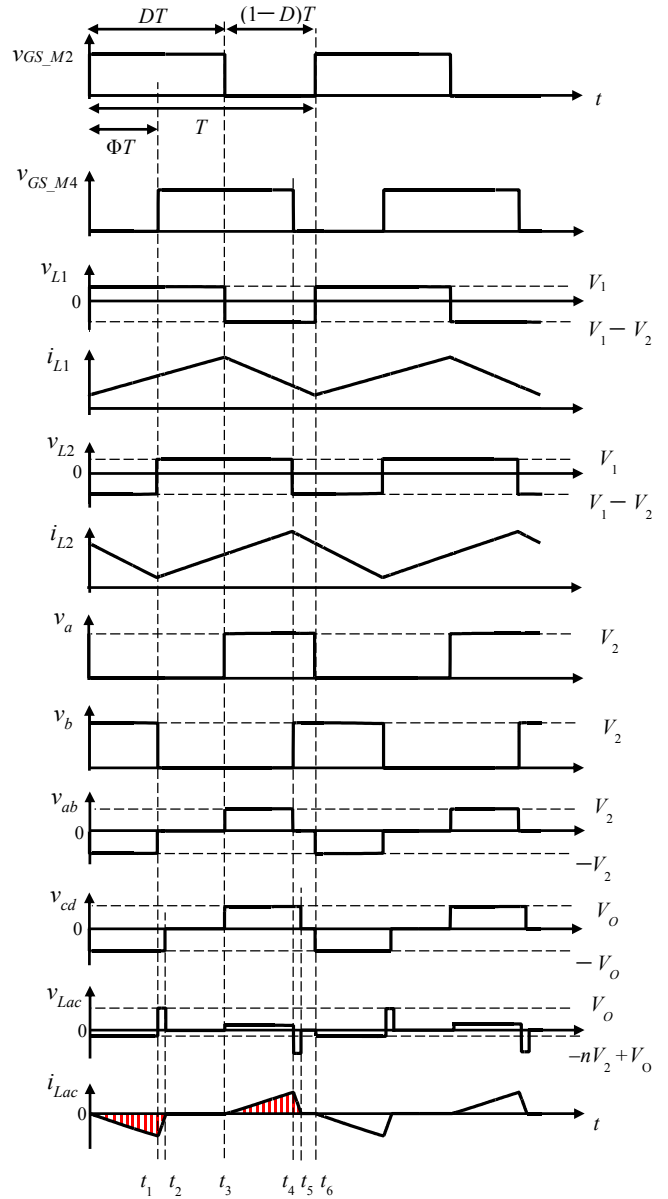


Fig. 3. Completely demagnetized ac inductor current key operating waveforms.

magnetized mode, the same current flowing through the ac inductor is flowing in the primary side and therefore, sent back to the source V_2 . Therefore, when the input voltage and the inductor current are not in phase reactive power is generated, which results in higher current stress in the converter primary side and, therefore, higher losses than in the completely demagnetized operating mode.

In the same way than the completely demagnetized operation mode, the partially and fully magnetized operation modes can be analysed by describing the converter operation intervals. By solving the equation relating the average of the rectified inductor current (13) and the load current (V_o/R_L), the output voltage of the converter operating in partially magnetized operation mode can be obtained.

$$I_{Lac,rec,avg} = \frac{V_o \Phi (\Phi(1-D)(M^2 - 2M - 1) - \Phi^2 - (1-D)^2)}{L_{ac} f (M+1)^2} \quad (13)$$

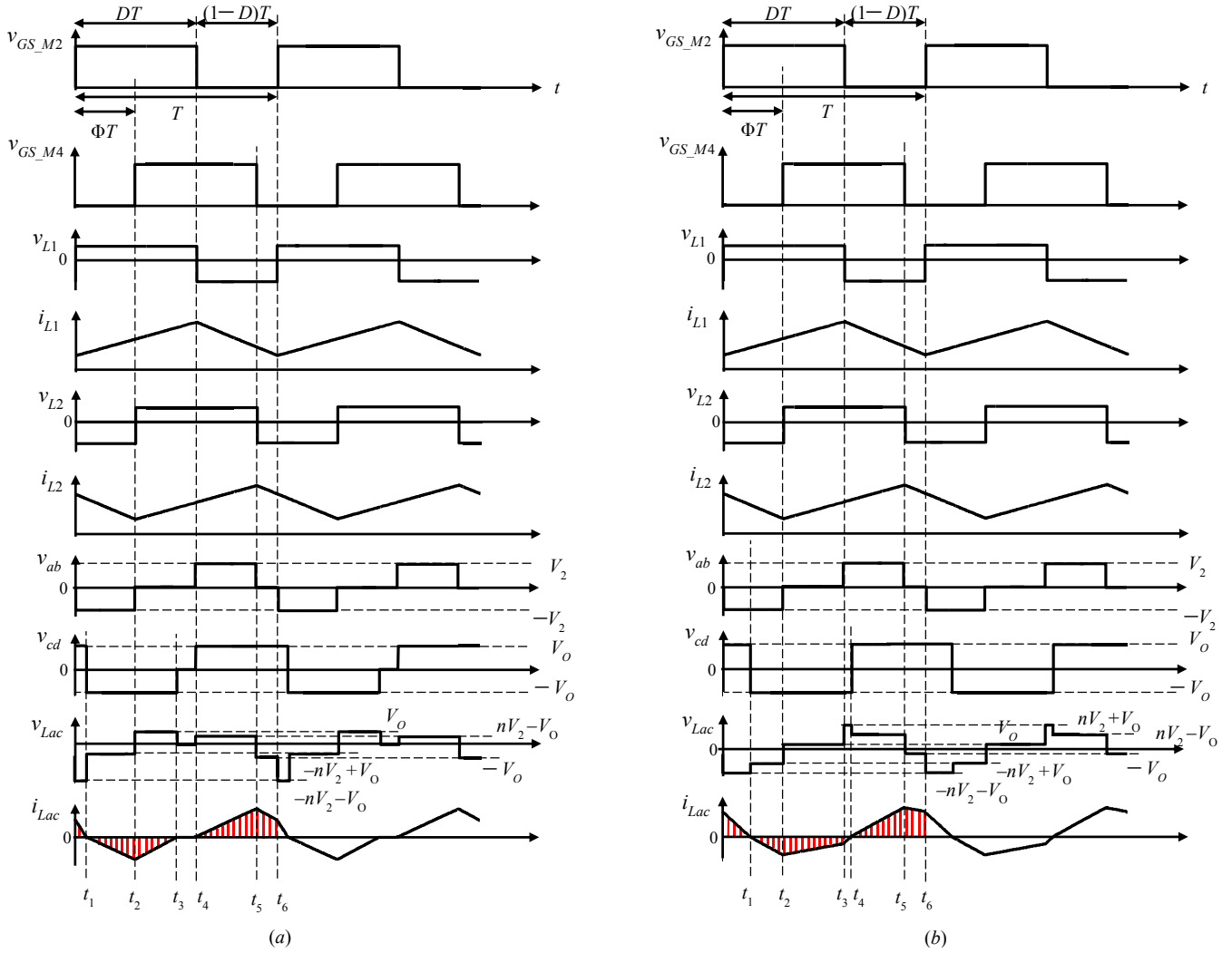


Fig. 4. (a) Partially magnetized ac inductor current key operating waveforms. (b) Fully magnetized ac inductor current key operating waveforms.

The time intervals corresponding to the fully magnetized operating mode can be calculated according to the waveforms shown in Fig. 4 (b), by solving the system of equations formed by the ac inductor volt-second balance and the rectified ac inductor current. By defining the interval $[0 \sim t_1]$ normalized to the period as shown in (14), the time intervals as a function of the phase-shift and the duty cycle parameters can be written as

$$\alpha = \frac{1}{4} \left(2D + 2\Phi + 2k - \sqrt{4D(1-D) + 4\Phi(1-\Phi) + 4k^2 - 1} \right) \quad (14)$$

$$t_1 = \alpha T \quad (15)$$

$$t_2 - t_1 = (\Phi - \alpha) \cdot T \quad (16)$$

$$t_3 - t_2 = (D - \Phi) \cdot T \quad (17)$$

$$t_4 - t_3 = \left(\alpha - D + \frac{1}{2} \right) \cdot T \quad (18)$$

$$t_5 - t_4 = \left(\Phi - \alpha + D - \frac{1}{2} \right) \cdot T \quad (19)$$

$$t_6 - t_5 = (1 - D - \Phi) \cdot T \quad (20)$$

The output voltage as a function of the phase-shift value and the duty cycle can be calculated by

$$V_o = nV_2 \left(-2k + \sqrt{4D(1-D) - 4\Phi(1-\Phi) + 4k^2 - 1} \right) \quad (21)$$

Partially and fully magnetized operation allow for higher power transfer for the same inductor value than the completely demagnetized mode. This is due to the increased charge per switching cycle delivered to the output capacitor, which can be observed in the highlighted area of the ac inductor current shown in Fig. 4 (a) and (b) compared to the completely demagnetized inductor current shown in Fig. 3. However, as discussed before, these operating modes move the current stress from the converter secondary to the primary side due to the generated reactive power, which acts in detriment of the efficiency in step up applications. Moreover, as it can be seen by comparing (7) and (21), when the converter leaves the completely demagnetized mode, the converter output voltage is no longer controlled solely by the phase-shift angle. This characteristic increases the difficulty in the implementation of the dual power flow converter control strategy. Considering all the aforementioned characteristics, completely demagnetized ac inductor current is the preferred operation mode.

III. DESIGN CONSIDERATIONS

In this section, design guidelines about the soft-switching operation and the *rms* current distribution of the primary switches for the completely demagnetized operation mode are discussed.

A. Soft-Switching Constraints

The proposed converter, unlike the conventional phase-shift full-bridge ZVS converter, has a relatively more complicated ZVS performance to analyse due to the input inductor currents i_{L1} and i_{L2} . ZVS can be deduced on the precondition that the anti-parallel diode of the MOSFET must conduct before the MOSFET is triggered. In other words, the main devices are turned-off with a positive current flowing and then the current diverts to the opposite diode, which allows the in-coming MOSFET to be switched-on under zero voltage condition. Therefore, the current flowing through MOSFETs $M_1 \sim M_4$ must be negative when the corresponding MOSFET is triggered. Taking into account the amount of stored energy in the MOSFETs' output capacitance (C_{OSS}), in order to obtain ZVS at turn-on the following relationships must be satisfied

$$\begin{cases} I_{L1,max} - ni_{Lac}(t_3) > I_{min} & \text{for } M_1 \\ I_{L1,min} - ni_{Lac}(t_0) < I_{min} & \text{for } M_2 \\ I_{L2,max} + ni_{Lac}(t_4) > I_{min} & \text{for } M_3 \\ I_{L2,min} + ni_{Lac}(t_1) < I_{min} & \text{for } M_4 \end{cases} \quad (22)$$

where

$$I_{Li,max} = \frac{P_1}{2V_1} + \frac{V_1(1-D)T}{2L_i} \quad (i=1,2) \quad (23)$$

$$I_{Li,min} = \frac{P_1}{2V_1} - \frac{V_1(1-D)T}{2L_i} \quad (i=1,2) \quad (24)$$

$$I_{min} = \sqrt{\frac{(2 \cdot C_{OSS}) \cdot V_2^2}{L_{ac}}} \quad (25)$$

As the waveforms shown in Fig. 4, where $\Phi < (1-D)$ and $D > 0.5$, when the input V_1 provides power to the load, M_2 in the leading half-bridge cannot operate under ZVS. However, M_4 in the lagging half-bridge can achieve ZVS if the constraints depicted in Fig. 5 are satisfied. As it can be observed in Fig. 5, as the power flow to the output port increases, the turn-on condition of M_4 moves towards the ZVS region due to the increased negative ac inductor peak current. However, increasing the power flow from the input port V_1 to the bidirectional port V_2 has the opposite effect due to an increased $I_{L2,min}$ value. It is important to observe the influence of the input inductor and ac inductor values on the switch ZVS region. Increasing both of the inductor values reduces the ZVS region, since $I_{L2,min}$ increases due to a reduced input inductor ripple current, and $ni_{Lac}(t_1)$ decreases for larger ac inductor values. Regarding the high side switches M_1 and M_3 , since they operate as synchronous rectifiers in the interleaved boost stage, both can operate under ZVS inherently, because the reflected ac inductor current, $ni_{Lac}(t_3)$, is equal to zero and $ni_{Lac}(t_4)$ is always positive.

A significant advantage of the proposed TPC topology is that the diodes on the secondary side can operate under ZCS conditions. As it can be observed in Fig. 3 and Fig. 4, the

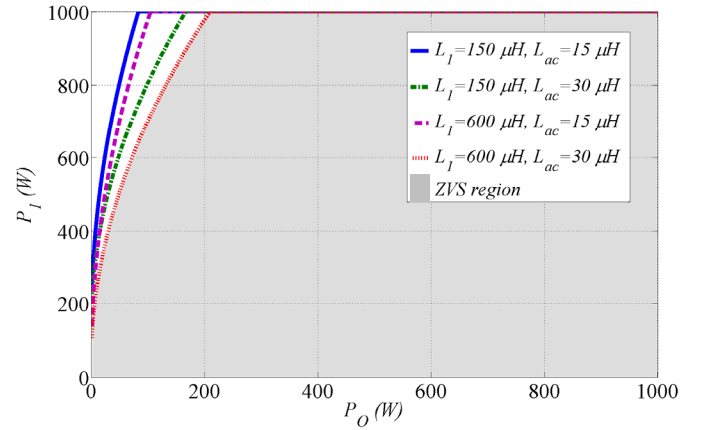


Fig. 5. ZVS range (operating conditions $V_1 = 50$ V, $V_2 = 100$ V and $V_o = 380$ V).

output bridge rectifier always changes its conduction state (edges of the waveform v_{cd}) when the ac inductor current reaches zero for all operating conditions. Therefore, due to the use of an ac inductor, the diodes on the secondary side always turn-off under ZCS conditions, which avoids the reverse recovery losses and makes it possible to use conventional silicon (Si) diodes.

B. Selection of MOSFETs and Diodes

Like all half-bridge boost derived converters, the current distribution in the primary side MOSFETs is unequal. In the proposed converter the analysis on the *rms* current distribution is more complex due to the variable phase-shift angle. If $\varphi = \pi$, the *rms* current of the MOSFETs can be calculated by,

$$I_{M1,rms} = I_{M3,rms} = \sqrt{nI_{Lac,rms}^2 - I_{L1,rms}^2} \quad (26)$$

$$I_{M2,rms} = I_{M4,rms} = \sqrt{nI_{Lac,rms}^2 + I_{L1,rms}^2} \quad (27)$$

According to the operating waveform of i_{Lac} shown in Fig. 3 and (1) – (4), the *rms* value of the ac inductor current can be obtained as

$$I_{Lac,rms} = I_{Lac,pk} \sqrt{\frac{2}{3}(\Phi + \beta)} \quad (28)$$

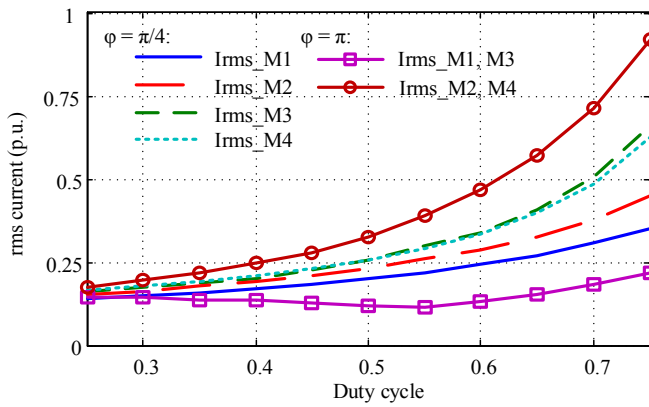
where $I_{Lac,pk} = I_{Lac}(t_4) = |I_{Lac}(t_1)|$ is given in (1).

Fig. 6 shows the switches' *rms* current as a function of duty cycle D . It can be found that for $\varphi = \pi$, M_2 and M_4 have the maximum *rms* current (worst case for M_2 and M_4), whereas M_1 and M_3 have the minimum *rms* current. Also, it can be observed that when $\varphi \neq \pi$, the current distribution will be more equal than the case $\varphi = \pi$. This phenomenon must be considered when choosing components and deciding thermal design for the proposed converter.

The current flowing through the diodes on the secondary side is distributed equally, and the average current in each diode can be calculated as

$$I_{D1,D4,avg} = I_{D2,D3,avg} = \frac{1}{2} \cdot I_{Lac,pk} \cdot (\Phi + \beta) \quad (29)$$

According to the operation principle analysis, the voltage stress over the MOSFETs is the maximum voltage of V_2 . The voltage stress across the diodes is the maximum output voltage owing to the voltage clamp effect by the output capacitor.

Fig. 6. Switches' rms current as a function of duty cycle D .

IV. STATE-SPACE MODELLING

In this section, state-space average modelling of the proposed TPC is presented. This technique to modelling switching dc-dc converters [30], which results in a dynamic linear model in terms of state-space equations, is used in this work. Due to the inherent sampling process of switched-mode converters, averaged models can accurately predict the behaviour up to half of the switching frequency [31]. If precise modelling beyond the switching frequency is required, i.e. in self-oscillating control schemes, a discrete-time approach for modelling switched-mode controllers can be used [32].

From the key operating waveforms illustrated in Fig. 3, it can be observed that the ac inductor charge and discharge always depends on the converter input voltage V_2 , the converter output voltage V_O and the phase-shift angle, whereas voltages V_1 and V_2 are regulated by the duty cycle. Therefore, the proposed topology can be dynamically modelled as two individual converters: a bidirectional interleaved boost converter, which balances the power flow within the two input sources, and a phase-shift full-bridge converter or single active bridge converter, which delivers the power to the load through the ac inductor. As a result, the proposed converter offers independent controllability by using duty cycle and phase-shift as control variables, and reutilizes the primary side switches to regulate the two power flows. The high integration of the two structures in a TPC results in a topology with lower component number and higher power density than multiple-converter systems. Moreover, as previously discussed, in the completely demagnetized case the energy transferred to the output port does not depend on the converter duty cycle; therefore, the two control variables, phase-shift Φ and duty-cycle D , are completely decoupled. Fig. 7 shows the integration of the bidirectional interleaved boost converter (BIBC) and the phase-shift full-bridge (PSFB) converter as a TPC topology.

As previously discussed, the completely demagnetized operation is the preferred operation mode, however, the converter can enter any of the other operating modes depending on the two input port voltages, the duty-cycle requirement and the output port loading conditions. Therefore, in order to ensure stability of the converter under all possible operating conditions, the dynamic modelling in the fully magnetized mode is also investigated.

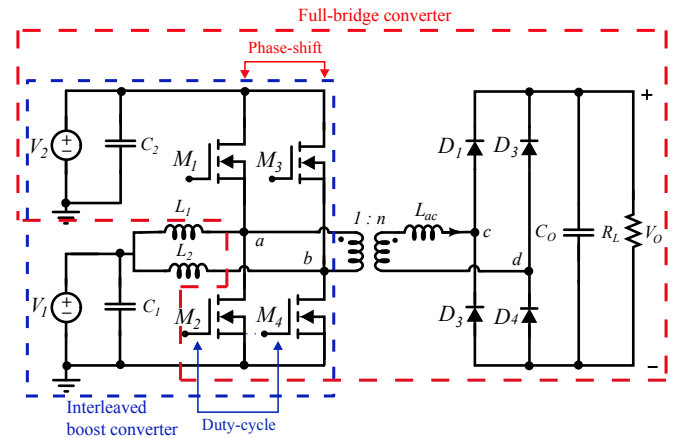
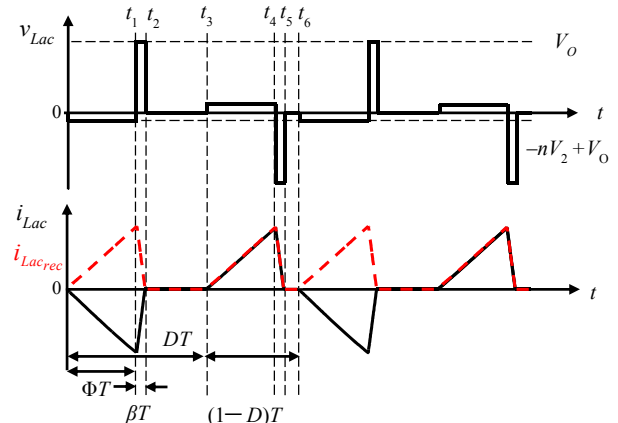


Fig. 7. Integration of the interleaved boost converter and phase-shift full-bridge converter as a TPC.

A. State-Space Modelling of the Phase-Shift Full-Bridge (PSFB) Converter

State-space average modelling of the phase-shift full-bridge (PSFB) converter is performed in this section. First, the completely demagnetized operating mode is analysed. The rectified ac inductor current and the output capacitor voltage are selected as state-variables, i.e. $x = [i_{Lac} \ v_{CO}]^T$. Fig. 8 shows the voltage and current across the ac inductor during the different switching states, together with the rectified ac inductor current. The state and input matrices are averaged over a period by multiplying them by the corresponding time interval. As shown in Fig. 3, there are six conduction states; however, since the state-variable is the rectified ac inductor current, the charge and discharge of the ac inductor during time intervals $[0 \sim t_1]$ and $[t_1 \sim t_2]$ is equivalent to time intervals $[t_3 \sim t_4]$ and $[t_4 \sim t_5]$, as shown in Fig. 8. Notice that because two control variables are used, duty cycle and phase-shift, time intervals $[t_2 \sim t_3]$ and $[t_5 \sim t_6]$ are not the same since they are related to D and $(1 - D)$, respectively.

The system is perturbed around a quiescent operating point $(X + \hat{x}, \Phi + \hat{\Phi}, \beta + \hat{\beta}, V_2 + \hat{v}_2)$ where $X \gg \hat{x}$, and linearized by neglecting the second order terms. Separating the dc and ac part of the linearized model, the steady-state operating point (30) and the small-signal model (31) are obtained.

Fig. 8. Voltage and current across the ac inductor L_{ac} (continuous) and rectified ac inductor current (dashed) in completely demagnetized operation mode.

$$X = \begin{bmatrix} I_{Lac} \\ V_{Co} \end{bmatrix} = -A^{-1}BV_2 = \begin{bmatrix} \frac{nV_2\Phi}{2R_L(\Phi+\beta)^2} \\ \frac{nV_2\Phi}{\Phi+\beta} \end{bmatrix} \quad (30)$$

$$\begin{aligned} \dot{\hat{x}} &= A\hat{x} + B\hat{v}_2 + [(2A_4 - 2A_6)X + (2B_4 - 2B_6)V_2]\hat{\Phi} + \\ &+ [(2A_5 - 2A_6)X + (2B_5 - 2B_6)V_2]\hat{\beta} \\ \dot{\hat{x}} &= \begin{bmatrix} 0 & -\frac{2(\Phi+\beta)}{L_{ac}} \\ \frac{2(\Phi+\beta)}{C_o} & -\frac{1}{C_oR_L} \end{bmatrix} \hat{x} + \begin{bmatrix} \frac{2n\Phi}{L_{ac}} \\ 0 \end{bmatrix} \hat{v}_2 + \\ &+ \begin{bmatrix} \frac{2nV_2\alpha}{L_{ac}(\Phi+\beta)} \\ \frac{nV_2\Phi}{C_oR_L(\Phi+\beta)^2} \end{bmatrix} \hat{\Phi} + \begin{bmatrix} -\frac{2nV_2\Phi}{L_{ac}(\Phi+\beta)} \\ \frac{nV_2\Phi}{C_oR_L(\Phi+\beta)^2} \end{bmatrix} \hat{\beta} \end{aligned} \quad (31)$$

where the averaged state and input matrices are given by

$$A = 2A_4\Phi + 2A_5\beta + A_6(1 - (2\Phi + 2\beta)) \quad (32)$$

$$B = 2B_4\Phi + 2B_5\beta + B_6(1 - (2\Phi + 2\beta)) \quad (33)$$

$$A_4 = \begin{bmatrix} 0 & -\frac{1}{L_{ac}} \\ \frac{1}{C_o} & -\frac{1}{R_L C_o} \end{bmatrix} \quad A_5 = \begin{bmatrix} 0 & -\frac{1}{L_{ac}} \\ \frac{1}{C_o} & -\frac{1}{R_L C_o} \end{bmatrix} \quad (34)$$

$$A_6 = \begin{bmatrix} 0 & 0 \\ 0 & -\frac{1}{R_L C_o} \end{bmatrix}$$

$$B_4 = \begin{bmatrix} \frac{n}{L_{ac}} \\ 0 \end{bmatrix} \quad B_5 = \begin{bmatrix} 0 \\ 0 \end{bmatrix} \quad B_6 = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

The discharge parameter β is defined in (3) and the phase-shift value Φ s given by

$$\Phi = \frac{V_o}{\sqrt{2}} \sqrt{\frac{-k}{nV_2(V_o - nV_2)}} \quad (35)$$

In order to obtain the dynamic model of the converter in the completely demagnetized mode, additional constraints need to be applied. The first constraint comes from the fact that the inductor current becomes zero for a portion of the switching period. Applying the constraint defined in (36) to the ac model presented in (31), leads to (37). As a result, the inductor dynamic equation turns into a static equation, as shown in (38), meaning that the ac inductor current does not behave as a true state-space variable since it loses its dynamic properties [33].

$$\frac{d\hat{i}_{Lac}}{dt} = 0 \quad (36)$$

$$\hat{\beta} = \frac{-(\Phi+\beta)}{V_o} \hat{v}_o + \frac{n\Phi}{V_o} \hat{v}_2 + \frac{nV_2\beta}{V_o(\Phi+\beta)} \hat{\Phi} \quad (37)$$

$$\begin{aligned} \dot{\hat{x}} &= \begin{bmatrix} 0 & 0 \\ \frac{2(\Phi+\beta)}{C_o} & -\frac{2}{C_oR_L} \end{bmatrix} \hat{x} + \begin{bmatrix} 0 \\ \frac{n\Phi}{C_oR_L(\Phi+\beta)} \end{bmatrix} \hat{v}_2 \\ &+ \begin{bmatrix} 0 \\ \frac{nV_2}{C_oR_L(\Phi+\beta)} \end{bmatrix} \hat{\Phi} \end{aligned} \quad (38)$$

The second constraint is obtained from the average of the inductor current as shown in (39).

$$i_{Lac} = f(v_2, v_o, \Phi, L_{ac}, T) = \frac{i_{Lac,pk}(nV_2 - V_o)\Phi}{2R_Lk} \quad (39)$$

The perturbation equation is found by taking the partial derivatives of (39) as shown in (40).

$$\begin{aligned} \hat{i}_{Lac} &= \frac{\partial i_{Lac}}{\partial v_o} \hat{v}_o + \frac{\partial i_{Lac}}{\partial v_2} \hat{v}_2 + \frac{\partial i_{Lac}}{\partial \Phi} \hat{\Phi} \\ \hat{i}_{Lac} &= \frac{\Phi}{R_Lk} \hat{v}_o + \frac{n\Phi}{R_Lk} \hat{v}_2 + \frac{(nV_2 - V_o)}{R_Lk} \hat{\Phi} \end{aligned} \quad (40)$$

By applying the perturbation equation (40) to (38), the phase-shift-to-output voltage transfer function in completely demagnetized mode is obtained (41). As previously discussed, in this operating mode the two control variables are decoupled and, therefore, the duty cycle control parameter has no direct effect on the regulation of the output voltage.

$$\begin{aligned} G_{v_o\Phi}(s) &= \frac{\hat{v}_o(s)}{\hat{\Phi}(s)} \Big|_{\hat{v}_2(s)=0} = \\ &= \frac{nV_2k + 2(\Phi+\beta)^2(nV_2 - V_o)}{(\Phi+\beta)} \cdot \frac{1}{sR_LC_o k + 2k + 2\Phi(\Phi+\beta)} \end{aligned} \quad (41)$$

In the same way, the audio susceptibility or line-to-output transfer function can be calculated as shown in (42).

$$\begin{aligned} G_{v_o v_2}(s) &= \frac{\hat{v}_o(s)}{\hat{v}_2(s)} \Big|_{\hat{\Phi}(s)=0} = \\ &= \frac{n\Phi k + 2n\Phi(\Phi+\beta)^2}{(\Phi+\beta)} \cdot \frac{1}{sR_LC_o k + 2k + 2\Phi(\Phi+\beta)} \end{aligned} \quad (42)$$

In order to ensure stability under all operating conditions, the dynamic behaviour of the TPC operating in the fully magnetized mode is also investigated. This operating mode is more complex than the completely demagnetized operation since no symmetry can be applied to the ac inductor waveform, as illustrated in Fig. 9.

As in the completely demagnetized operating mode, in the fully magnetized mode the state-variables are the rectified ac inductor current and the output capacitor voltage. The dynamic equation of the capacitor C_o is expressed in terms of conservation of charge [36], [37] in order to take into account the correct charge applied to the output capacitor and accurately describe the dynamics involved in the rectified inductor current. By using the time intervals defined in (14) – (20) the input and state matrices for the six time intervals can be written as (43).

$$\begin{aligned}
 A_1 &= \begin{bmatrix} 0 & -\frac{1}{L_{ac}} \\ 0 & \frac{\alpha T}{2L_{ac}C_o} - \frac{1}{R_L C_o} \end{bmatrix} & A_2 &= \begin{bmatrix} 0 & -\frac{1}{L_{ac}} \\ 0 & \frac{(\Phi - \alpha)T}{2L_{ac}C_o} - \frac{1}{R_L C_o} \end{bmatrix} & A_3 &= \begin{bmatrix} 0 & -\frac{1}{L_{ac}} \\ 0 & \frac{(D - \Phi)T}{2L_{ac}C_o} + \frac{(\alpha - D + 1/2)T}{L_{ac}C_o} - \frac{1}{R_L C_o} \end{bmatrix} \\
 A_4 &= \begin{bmatrix} 0 & -\frac{1}{L_{ac}} \\ 0 & \frac{(\alpha - D + 1/2)T}{2L_{ac}C_o} - \frac{1}{R_L C_o} \end{bmatrix} & A_5 &= \begin{bmatrix} 0 & -\frac{1}{L_{ac}} \\ 0 & \frac{(\Phi - \alpha + D - 1/2)T}{2L_{ac}C_o} - \frac{1}{R_L C_o} \end{bmatrix} & A_6 &= \begin{bmatrix} 0 & -\frac{1}{L_{ac}} \\ 0 & \frac{(1 - D - \Phi)T}{2L_{ac}C_o} + \frac{\alpha T}{L_{ac}C_o} - \frac{1}{R_L C_o} \end{bmatrix} \\
 B_1 &= \begin{bmatrix} -\frac{n}{L_{ac}} \\ \frac{\alpha n T}{2L_{ac}C_o} \end{bmatrix} & B_2 &= \begin{bmatrix} \frac{n}{L_{ac}} \\ \frac{(\Phi - \alpha)n T}{2L_{ac}C_o} \end{bmatrix} & B_3 &= \begin{bmatrix} 0 \\ \frac{n(\alpha - D + 1/2)T}{2L_{ac}C_o} \end{bmatrix} \\
 B_4 &= \begin{bmatrix} -\frac{n}{L_{ac}} \\ \frac{n(\alpha - D + 1/2)T}{2L_{ac}C_o} \end{bmatrix} & B_5 &= \begin{bmatrix} \frac{n}{L_{ac}} \\ \frac{(\Phi - \alpha + D - 1/2)n T}{2L_{ac}C_o} \end{bmatrix} & B_6 &= \begin{bmatrix} 0 \\ \frac{\alpha n T}{2L_{ac}C_o} \end{bmatrix}
 \end{aligned} \tag{43}$$

$$A = A_1\alpha + A_2(\Phi - \alpha) + A_3(D - \Phi) + A_4(\alpha - D + 1/2) + A_5(\Phi - \alpha + D - 1/2) + A_6(1 - D - \Phi) \tag{44}$$

$$B = B_1\alpha + B_2(\Phi - \alpha) + B_3(D - \Phi) + B_4(\alpha - D + 1/2) + B_5(\Phi - \alpha + D - 1/2) + B_6(1 - D - \Phi) \tag{45}$$

The state and input matrices are averaged over a period, by using the time intervals defined in (14) – (20), as shown in (44) and (45).

The system is linearized by using the Jacobian linearization as

$$\dot{\hat{x}} = A_{alt}\hat{x} + B_{alt}\hat{u} \tag{46}$$

where the Jacobian matrices (47) are defined as the derivatives of the inductor and capacitor differential equations at the linearization point (48).

$$A_{alt} = \begin{bmatrix} \frac{\partial f_1}{\partial i_{Lac}} & \frac{\partial f_1}{\partial v_{Co}} \\ \frac{\partial f_2}{\partial i_{Lac}} & \frac{\partial f_2}{\partial v_{Co}} \end{bmatrix} \bigg|_{\substack{i_{Lac}=I_{Lac} \\ v_{Co}=V_o}} \tag{47}$$

$$B_{alt} = \begin{bmatrix} \frac{\partial f_1}{\partial u_2} \\ \frac{\partial f_2}{\partial u_2} \end{bmatrix} \bigg|_{u_2=V_2} \quad E_{alt} = \begin{bmatrix} \frac{\partial f_1}{\partial \Phi} \\ \frac{\partial f_2}{\partial \Phi} \end{bmatrix} \bigg|_{\Phi=\Phi}$$

$$\begin{bmatrix} \frac{di_{Lac}}{dt} \\ \frac{dv_{Co}}{dt} \end{bmatrix} = \begin{bmatrix} A_{11} & A_{12} \\ A_{21} & A_{22} \end{bmatrix} \begin{bmatrix} i_{Lac} \\ v_{Co} \end{bmatrix} + \begin{bmatrix} B_1 \\ B_2 \end{bmatrix} u_2 \tag{48}$$

$$f_1 = \frac{di_{Lac}}{dt} = A_{11}i_{Lac} + A_{12}v_{Co} + B_1u_2$$

$$f_2 = \frac{dv_{Co}}{dt} = A_{21}i_{Lac} + A_{22}v_{Co} + B_2u_2$$

The state-variable-to-phase-shift transfer function is obtained as

$$G_{x\Phi}(s) = \frac{\hat{x}(s)}{\hat{\Phi}(s)} \bigg|_{\substack{\hat{u}_2(s)=0 \\ \hat{d}(s)=0}} = [sI - A_{alt}]^{-1} \cdot E_{alt} \tag{49}$$

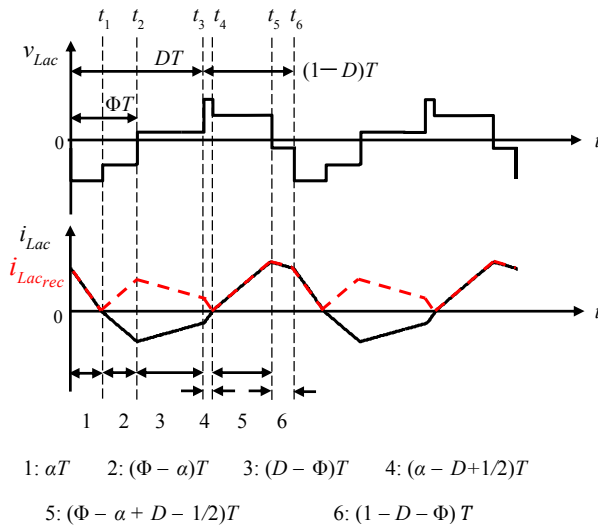


Fig. 9. Voltage and current across the ac inductor L_{ac} (continuous) and rectified ac inductor current (dashed) in fully magnetized operation mode.

In the same way, by using (46) to (49) and calculating the partial derivatives respect to the duty cycle instead of the phase-shift, the duty-cycle-to-output voltage transfer function for the fully magnetized operation mode can be obtained.

B. State-Space Modelling of the Bidirectional Interleaved Boost Converter (BIBC)

In this section, state-space modelling of the BIBC, which operates in continuous conduction mode (CCM), is performed. The circuit diagram of the converter is shown in Fig. 10. The input ports, V_1 and V_2 , interface with the renewable energy source and energy storage, respectively. Hence, the primary side of the proposed topology can be seen as an interleaved boost or buck converter depending on the direction of the power flow. In the case of a photovoltaic (PV) panel as the renewable energy source, the control variable will be taken as the converter input voltage, since the PV voltage does not present strong variations with irradiation changes [38]. In the case of a fuel cell, input current control will be selected in order to operate the fuel cell at a constant load level. Moreover, the parameters of the energy storage port can be monitored and the control scheme changed to voltage or current control on the battery depending on its state of charge (SOC).

The state-space modelling of the BIBC is performed with ideal components; nevertheless, both ports V_1 and V_2 , are modelled as an ideal voltage source with a series resistance in order to account for the dynamic resistance of the renewable energy source or the energy storage element. The state-space vector is chosen as $x = [i_L \ v_{C1} \ v_{C2}]^T$. The converter presents two switching intervals depending on the position of the switches M_2 and M_4 . The state, input, output and direct transmission matrices, A , B , C , D , respectively, for each subinterval (50), (51), are averaged over a period by multiplying by each switching interval duty cycle, (52) and expressed in terms of the state-space equation, as shown in (53) and (54).

$$A_1 = \begin{bmatrix} 0 & \frac{1}{L_1} + \frac{1}{L_2} & 0 \\ -\frac{1}{C_1} & -\frac{1}{R_1 C_1} & 0 \\ 0 & 0 & -\frac{1}{R_2 C_2} \end{bmatrix} \quad B_1 = \begin{bmatrix} 0 & 0 \\ \frac{1}{R_1 C_1} & 0 \\ 0 & \frac{1}{R_2 C_2} \end{bmatrix} \quad (50)$$

$$C_1 = [0 \ 0 \ 1] \quad D_1 = [0 \ 0]$$

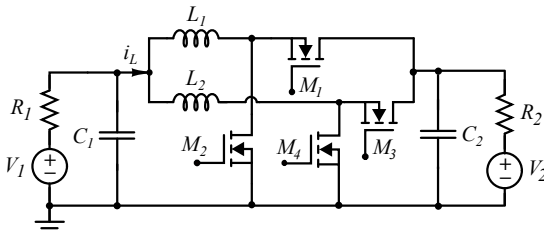


Fig. 10. Bidirectional interleaved boost converter BIBC.

$$A_2 = \begin{bmatrix} 0 & \frac{1}{L_1} + \frac{1}{L_2} & -\frac{1}{L_1} - \frac{1}{L_2} \\ -\frac{1}{C_1} & -\frac{1}{R_1 C_1} & 0 \\ \frac{1}{C_2} & 0 & -\frac{1}{R_2 C_2} \end{bmatrix} \quad B_2 = \begin{bmatrix} 0 & 0 \\ \frac{1}{R_1 C_1} & 0 \\ 0 & \frac{1}{R_2 C_2} \end{bmatrix} \quad (51)$$

$$C_2 = [0 \ 0 \ 1] \quad D_2 = [0 \ 0]$$

$$A = A_1 D + A_2 (1 - D) \\ B = B_1 D + B_2 (1 - D) \quad (52)$$

$$C = C_1 D + C_2 (1 - D) \\ D = D_1 D + D_2 (1 - D) \\ \dot{x} = Ax + Bu \quad (53)$$

$$y = Cx + Du \quad (54)$$

After the perturbation and linearization, the duty-cycle to state-variable (55) and the steady-state (dc) operating point (56) are obtained. From (55), the controllers for voltage and current regulation of the renewable energy and the energy storage port can be designed accordingly.

$$\hat{x} = (sI - A)^{-1} \cdot [(A_1 - A_2)X + (B_1 - B_2)U] \quad (55)$$

$$X = -A^{-1} \cdot B \cdot U \quad (56)$$

The audio susceptibility transfer function is calculated as (57).

$$G_{v_{2v1}}(s) = \left. \frac{\hat{v}_2(s)}{\hat{v}_1(s)} \right|_{\hat{d}(s)=0} = C(sI - A)^{-1} \cdot B \quad (57)$$

In the BIBC, the variation of the phase-shift angle will only affect the input current ripple; therefore, it does not have an effect on the averaged current, and consequently, on the duty-cycle-to-inductor current transfer function.

V. POWER FLOW REGULATION AND CONTROL

The block diagram of the designed power management and feedback regulators is shown in Fig. 11. Four different controllers are designed for the energy management of the renewable power system. At the renewable energy port, either voltage or current can be selected to be regulated depending on the type of the selected renewable energy source. At the energy storage port, constant voltage (CV) and constant current (CI) regulators are implemented, and at the output port, voltage regulation is performed. In order to control the power among the two inputs and the load and thereby balance the power between the different energy sources, two control loops are active at any time. The output port regulation loop is employed to regulate the load voltage by the phase-shift angle Φ . On the other hand, assuming V_1 is the renewable energy source such as fuel cells or photovoltaics, the voltage or current is controlled by the duty cycle D . The power from the other input V_2 as an energy storage unit, for example a battery or a super-capacitor, is controlled depending on the power at the renewable energy source and the output load power

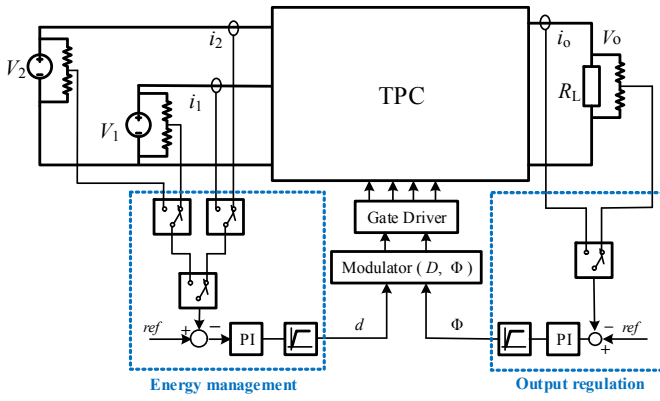


Fig. 11. Block diagram of energy/power management and control.

demand. Therefore, the energy management and control scheme can be summarized in the following way. The system is always set to control the renewable energy source and in the case of a photovoltaic application, to maximize the power delivered to the system through a maximum power point tracking algorithm (MPPT). If the renewable input power is smaller than the required power at the output port, the storage unit will compensate the power difference automatically. On the other hand, if the input power is bigger than the power required at the load terminal, the energy surplus is used to charge the energy storage element by inverting the power flow direction at this port. The state-of-charge (SOC) of the energy storage element is always being monitored and when it is above or below its recommended values, the system is set to control the bidirectional port by performing CV or CI control, until the energy storage element SOC allows for a change in the operation mode.

VI. EXPERIMENTAL RESULTS

The proposed TPC has been simulated, designed, built and tested to validate the previous theoretical analysis including the derived small-signal models. Fig. 12 shows the experimental prototype of the proposed TPC topology, which is constructed with a fast prototyping technique. The converter is designed to interface with hybrid renewable energy systems, i.e. operating a single phase grid-tie or as stand-alone dc microgrid power system. The specifications and the components employed in the construction of the prototype are listed in Table I. The control law is implemented by means of a digital signal processor (DSP) TMS320F28035 to generate the four gate signals with an adjustable duty cycle and phase-shift angle. The currents at the input and output ports are measured with Hall Effect current transducers LEM LA55-P, LA25-NP respectively.

Fig. 13 illustrates the measured waveforms of the PWM signal v_{GS-M2} and v_{GS-M4} and the two phase-shifted inductor currents i_{L1} and i_{L2} .

According to the waveforms of ZVS operation shown in Fig. 14, the drain to source voltage v_{DS-M3} and v_{DS-M4} have completely decreased to zero before switches M_3 and M_4 are turned-on, and there are no transient voltage spikes and rings across the switches. Therefore, the converter will have close to zero switching losses and low electromagnetic emissions.

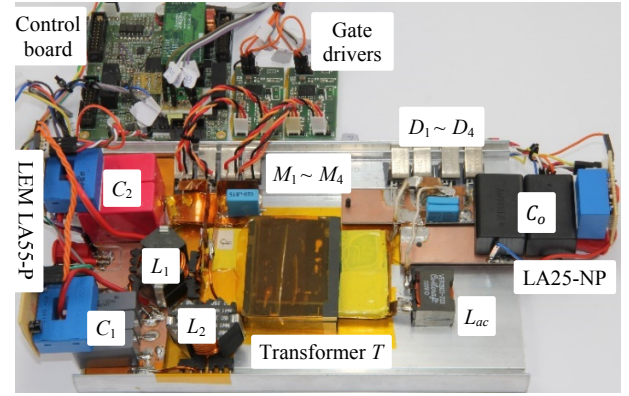


Fig. 12. Experimental prototype of the proposed TPC topology.

TABLE I
SYSTEM SPECIFICATIONS AND COMPONENTS

Input voltage	$V_1 = 25 - 60$ V
	$V_2_{max} = 120$ V
Output voltage	$V_O = 300 \sim 380$ V
Maximum output power	$P_{Omax} = 1000$ W
$M_1 \sim M_4$	IRFB4115 (150 V / 104 A)
$D_1 \sim D_4$	HFA08TB60 (600 V / 8 A)
Transformer T	4:16, ELP64/10/50 Ferrite N87
Inductors L_1 and L_2	155 μ H N41 gapped core RM12
Inductor L_{ac}	28 μ H Coilcraft VER2923-223
Capacitor C_1	2×10 μ F 160 V WIMA MKP4
Capacitor C_2	3×22 μ F 63 V AV MKT
Capacitor C_O	2×10 μ F 700 V VISHAY MKP
Switching frequency	$f = 60$ kHz
Digital controller	TMS320F28035 DSP

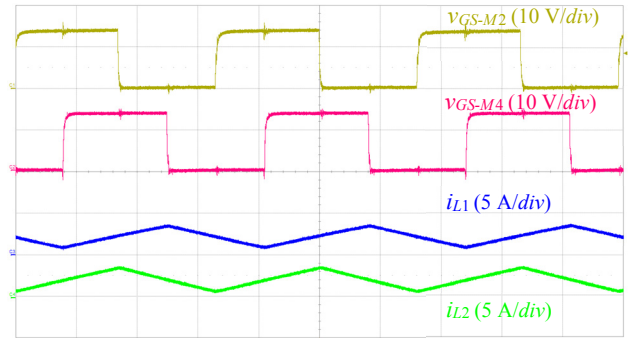


Fig. 13. Experimental results of the phase-shifted gate-source voltage of M_2 and M_4 and the inductor currents i_{L1} and i_{L2} operating in DI mode at $V_1 = 50$ V, $V_2 = 100$ V and $V_O = 370$ V, $P_O = 400$ W, $P_1 = 200$ W, $P_2 = 200$ W. Time scale: 5 μ s/div.

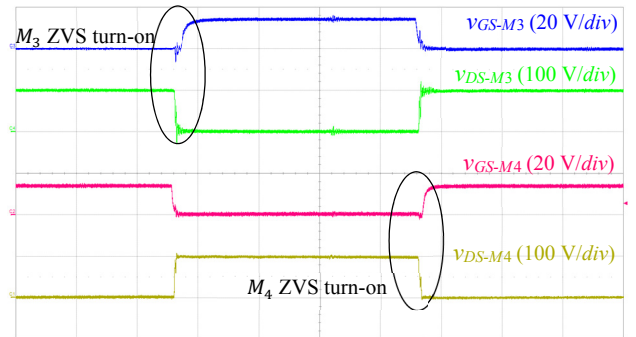


Fig. 14. Experimental results of the gate voltage and drain voltage of M_3 and M_4 at $V_1 = 50$ V, $V_2 = 100$ V and $V_O = 370$ V, $P_1 = 100$ W, $P_2 = 100$ W, $P_O = 200$ W. Time scale: 2 μ s/div.

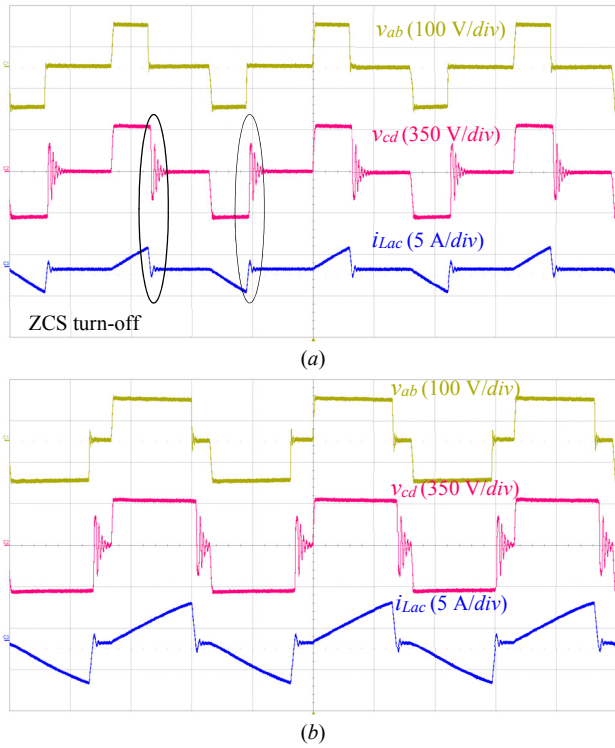


Fig. 15. Experimental results of the high frequency ac voltages v_{ab} , v_{cd} and inductor current i_{Lac} operating in DI mode at $V_1 = 50$ V, $V_2 = 100$ V and $V_O = 370$ V (a) $P_O = 200$ W, $P_1 = 100$ W, $P_2 = 100$ W. (b) $P_O = 800$ W, $P_1 = 100$ W, $P_2 = 700$ W. Time scale: $5 \mu\text{s/div}$.

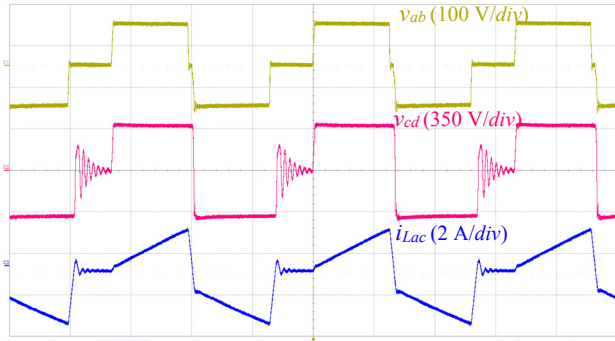


Fig. 16. Experimental waveforms of v_{ab} , v_{cd} and partially magnetized i_{Lac} operating in DI mode at $V_1 = 40$ V, $V_2 = 100$ V and $V_O = 370$ V, $P_1 = 100$ W, $P_2 = 300$ W, $P_O = 400$ W. Time scale: $5 \mu\text{s/div}$.

Fig. 15 (a) and (b) shows the measured high frequency ac voltages v_{ab} , v_{cd} and inductor current i_{Lac} of the converter operating in DI mode at different output power levels, respectively. It can be found that by using the capacitor C_2 and high side switches M_1 and M_3 as an active clamp circuit, the voltage transient spike across the current-fed bridge is suppressed.

The ZCS operation of the output diodes can be observed in the high frequency ac voltage v_{Lac} and current i_{Lac} shown in Fig. 15. As discussed in section III, due to the use of an ac inductor, the output bridge rectifier always changes its conduction state when the ac inductor current reaches zero, and therefore, the diodes always turn-off under ZCS conditions. A high frequency oscillation in the ac voltage v_{cd} can also be observed in Fig. 15. As in any discontinuous conduction mode (DCM) converter operation, when the inductor current reaches zero, a resonance between the bridge

rectifier parasitic capacitance and the ac inductor magnetizing inductance occurs. The energy stored in the diodes' parasitic capacitance will be dissipated in the circuit as joule losses. This loss, independent of the converter output power, is calculated to be 16 mW, for $V_D = V_O = 380$ V, according to the junction capacitance value given in the component's datasheet.

As an example, if a larger ac inductor is used ($66 \mu\text{H}$), the ac inductor current becomes partially magnetized. The experimental waveforms in this operating mode are presented in Fig. 16, where it can be seen that the ac inductor current does not stay at zero level before starting the next charging subinterval, as in the key operating waveform shown in Fig. 4.

Fig. 17 (a) and (b) shows the measured efficiency curves of the TPC topology operating in DI, DO and SISO modes at $V_1 = 50$ V, $V_2 = 100$ V and $V_O = 370$ V. The efficiency measurement is performed with the converter operating in closed loop with a dc power supply connected in parallel to an electronic load at the bidirectional port. The electronic load is configured in constant voltage (CV) mode to simulate the behaviour of a battery. As it can be observed, when the converter operates in DO mode, the efficiency increases as the power flow moves from the output port (SISO $V_1 V_O$) towards the bidirectional port (SISO $V_1 V_2$). This is due to the fact that the energy is processed only by the non-isolated interleaved boost converter instead of being boosted to V_2 and transferred through the transformer to the output port V_O . A peak

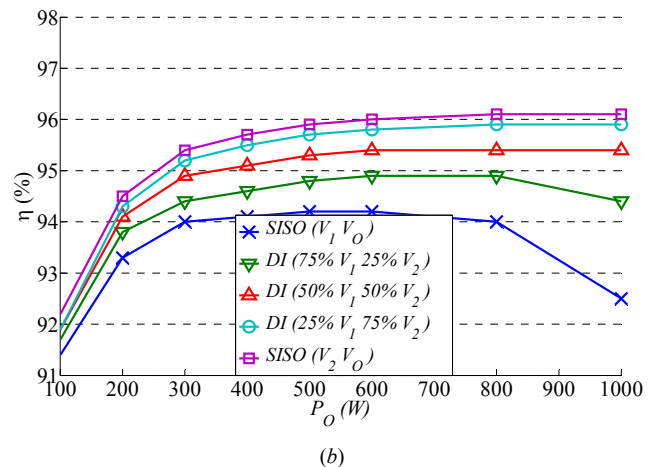
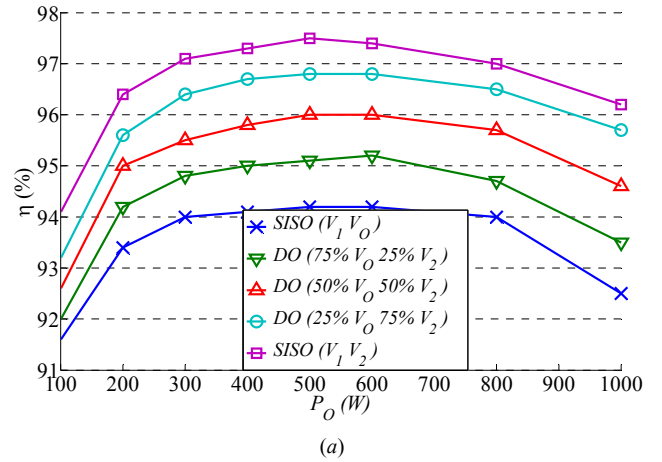


Fig. 17. Measured efficiency curves of the converter in DI, DO and SISO modes at $V_1 = 50$ V, $V_2 = 100$ V and $V_O = 370$ V.

efficiency of 97.5% is achieved in SISO V_1V_2 , whereas the maximum achieved efficiency in SISO V_1V_O mode is 94.2%. The same behavior is observed when the converter operates in DI mode and the operation changes from SISO V_1V_O to SISO V_2V_O . In this case, SISO V_2V_O shows higher efficiency than SISO V_1V_O due to the energy being processed once through the phase-shift isolated stage instead of being boosted from V_1 to V_2 and then transferred to the output through the isolated stage. The maximum efficiency achieved in SISO V_2V_O mode is 96.1%.

In order to validate the mathematical modelling performed in section IV, the calculated control and input transfer functions are compared to LTspice simulations [34], [35], as well as experimental measurements. The dynamic behaviour of the TPC is measured with a vector network analyser (VNA) OmicronLab Bode100. Fig. 18 shows the calculated, simulated and measured phase-shift-to-output voltage transfer function of the PSFB converter operating in completely demagnetized mode under the following conditions: $V_2 = 50$ V, $V_O = 100$ V, $R_L = 100$ Ω , $P_O = 100$ W, $\Phi = 0.17\pi$. As it can be observed, the mathematical model shows very good match with the simulation and the experimental results.

As in the completely demagnetized mode, in order to validate the mathematical model of the PSFB operating in fully magnetized operation, the circuit is simulated in LTspice and the result is compared to the mathematical model, as shown in Fig. 19. The simulation and the calculation are performed under the following conditions: $V_2 = 50$ V, $V_O = 100$ V, $R_L = 10$ Ω , $P_O = 1000$ W, $\Phi = 0.74\pi$, $D = 0.6$. As it can be observed, in the fully magnetized mode, the system behaves as a first order system, since the inductor current dynamics contributes very little to the control-to-output transfer function. This is due to the fact that the inductor current is an ac waveform, which makes the dynamics of this state-variable only visible at high frequencies. The control-to-output transfer function in fully magnetized mode is, therefore similar to the demagnetized operation; however, in this case, the gain is reduced due to the increased output load. As observed in Fig. 19, the proposed mathematical model shows good match with the simulation results. On the other hand, the duty cycle-to-output voltage transfer function gain is several

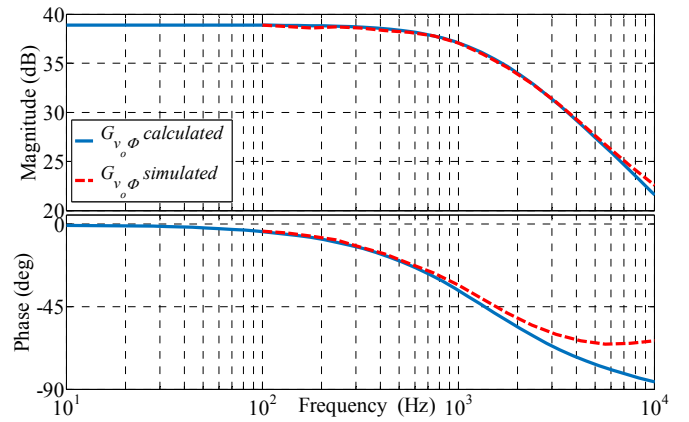


Fig. 19. PSFB fully magnetized ac inductor current phase-shift-to-output voltage ($G_{v_o\phi}$) transfer function calculated (continuous line) and measured (dashed line).

orders of magnitude smaller than the phase-shift-to-output voltage transfer function gain. Therefore, the perturbations on the duty cycle due to the regulation of the power flow between V_1 and V_2 , will have very small effect on the regulation of the converter output voltage. Since the plant transfer function behaves similarly to the demagnetized mode, and no special consideration need to be taken into account to suppress perturbations due to variations in the converter duty cycle, it can be concluded that entering this mode will not present any stability issues.

Once the validity of the model is verified, a compensation for the PSFB converter operating in completely demagnetized mode is designed. The compensation consists of an integrator and a zero placed at the resonant frequency of the plant transfer function. Fig. 20 shows the PSFB converter calculated and measured loop-gain for the designed controller with a crossover frequency of $f_c = 2.29$ kHz and phase margin $PM = 40^\circ$. As it can be observed in Fig. 20, the loop gain measurement presents very close match with the mathematical calculation.

As in the PSFB case, in order to validate the mathematical modelling of the BIBC duty-cycle-to-inductor current transfer measurement is performed with the converter working with a

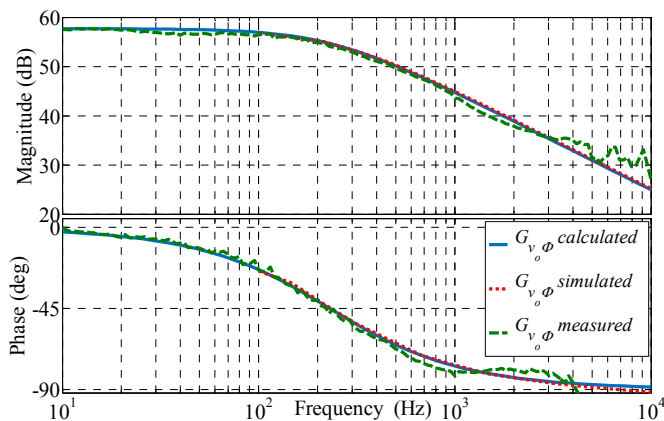


Fig. 18. PSFB completely demagnetized ac inductor current phase-shift-to-output voltage ($G_{v_o\phi}$) transfer function calculated (continuous line), simulated (dotted line) and measured (dashed line).

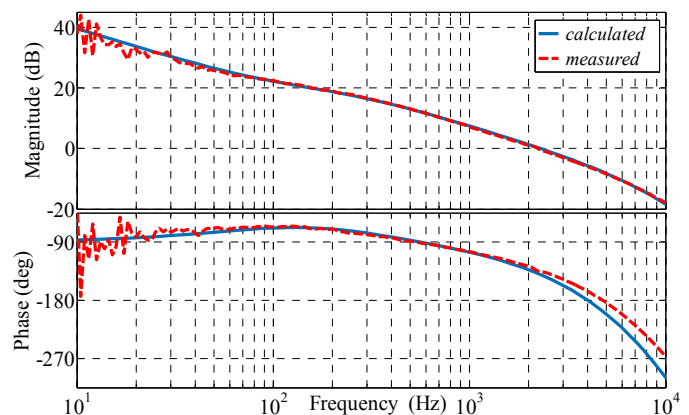


Fig. 20. PSFB completely demagnetized ac inductor current phase-shift-to-output voltage loop-gain transfer function calculated (continuous line) and measured (dashed line).

resistive load instead of with an electronic load configured in CV mode. Measuring any transfer function with an electronic load is not recommended since the control circuit of the electronic load can interfere with the converter under test. Notice that the BIBC plant transfer function differs when is operated with a battery or with a resistive load. This can be observed from the calculated and simulated duty-cycle-to-inductor current transfer function shown in Fig. 21 (a) for battery load, and the measured transfer function with a resistive load, shown Fig. 21 (b), for the same converter power level. The complex poles appearing at the converter natural resonant frequency in the resistive load case are split in the case of battery loading, which make the battery load case to behave as a first order system. Fig. 21 (a) shows the calculated and simulated duty-cycle-to-inductor current transfer function with a battery as a load under the following operating conditions: $V_1 = 25$ V, $R_l = 150$ m Ω , $V_2 = 50$ V, $R_2 = 25$ Ω , $I_L = 4$ A, $P_2 = 100$ W, $D = 0.513$. Fig. 21 (b) shows the measurement of the BIBC duty-cycle-to-inductor current transfer function with resistive load under the following conditions: $V_1 = 25$ V, $R_l = 150$ m Ω , $V_2 = 50$ V, $R_2 = 100$

m Ω , $I_L = 4$ A, $P_2 = 100$ W, $D = 0.513$. As it can be observed from the results presented in Fig. 21, the mathematical model shows very good match with the performed simulation and measurement. A compensation for the BIBC operating with a battery at the bidirectional port V_2 is designed. The compensation consisting of an integrator and a zero is designed and tested; nevertheless, the measurement results are not shown due to the aforementioned reasons.

The audio susceptibilities of the separate converters as well as the combination as a TPC topology are investigated. The audio susceptibility, or line-to-output transfer function, relates how variations at the input port will affect the output as a function of the frequency; hence, the interaction between the two control loops within the proposed topology can be examined. Fig. 22 (a) and (b) present the calculated and measured audio susceptibility transfer functions of the PSFB converter and the BIBC, respectively, under the conditions: $V_1 = 25$ V, $R_l = 150$ m Ω , $V_2 = 50$ V, $R_2 = 50$ Ω , $I_L = 2$ A, $P_2 = 50$ W, $D = 0.513$, where a Picotest J2120 is used to inject up to 50 V input voltage and 5 A input current. As it can be observed the measurements show close match with the proposed model.

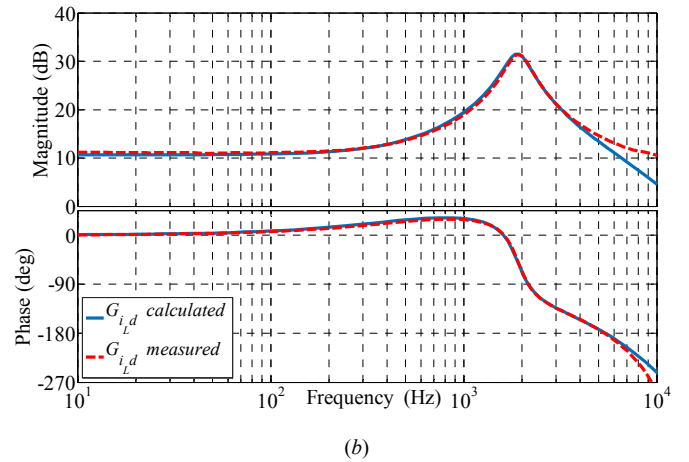
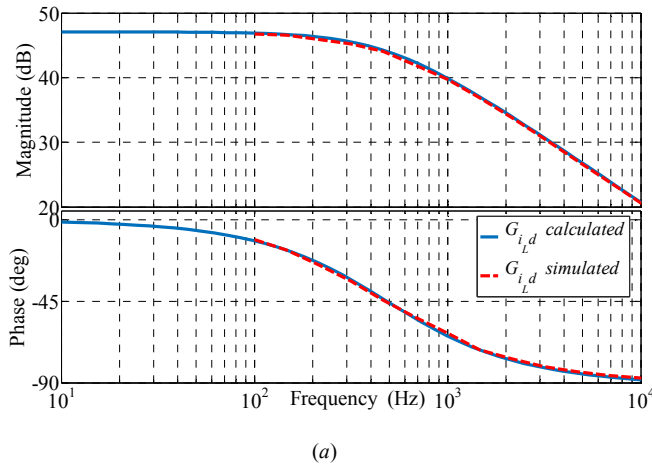


Fig. 21. BIBC duty-cycle-to-inductor current (G_{i_d}) transfer function: (a) operated with a battery as a load calculated (continuous line) and simulated (dashed line) and (b) operated with a resistive load, calculated (continuous line) and measured (dashed line).

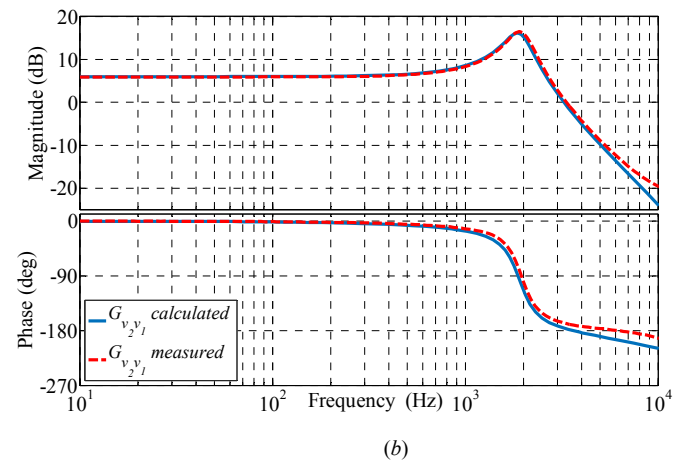
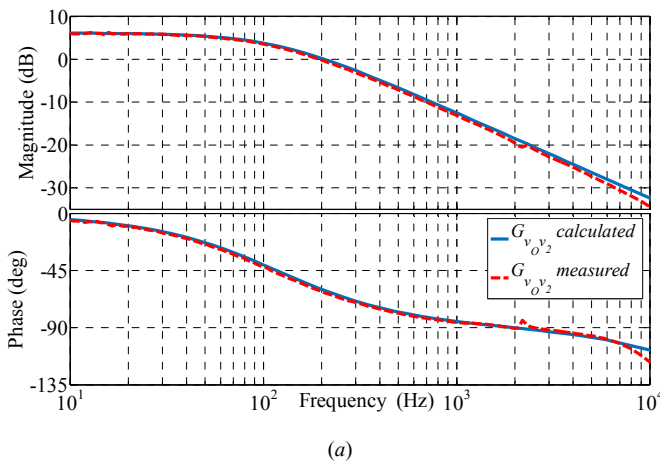


Fig. 22. Calculated (continuous line) and measured (dashed line) audio susceptibility transfer functions: (a) PSFB audio susceptibility ($G_{v_o v_2}$), (b) BIBC audio susceptibility ($G_{v_2 v_1}$).

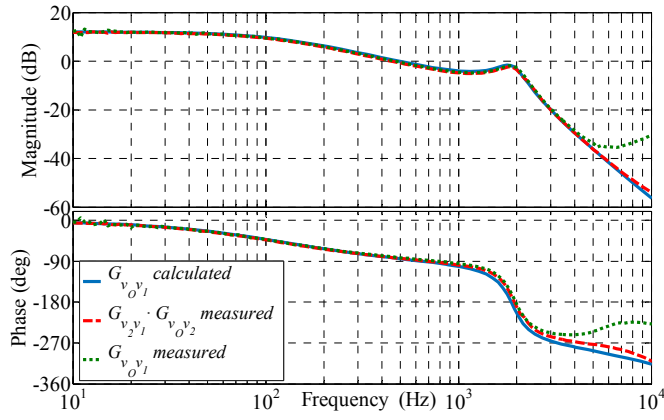


Fig. 23. Calculated (continuous line) and measured (dashed lines) TPC audio susceptibility (G_{v_o/v_1}) transfer function.

Fig. 23 shows the calculated and measured line-to-output transfer function of the TCP (from the input port V_1 to the output port V_O), measured under the following conditions: $V_1 = 25$ V, $R_L = 150$ m Ω , $V_2 = 50$ V, $R_2 = 50$ Ω , $I_L = 2$ A, $P_2 = 50$ W, $D = 0.513$, $V_O = 100$ V, $R_L = 200$ Ω , $P_O = 50$ W, $\Phi = 0.17\pi$. The calculated transfer function is obtained as the series combination of the individual transfer functions (58).

$$G_{v_o/v_1}(s) = G_{v_2/v_1}(s) \cdot G_{v_o/v_2}(s) = \left. \frac{\hat{v}_2(s)}{\hat{v}_1(s)} \right|_{\hat{d}(s)=0} \cdot \left. \frac{\hat{v}_o(s)}{\hat{v}_2(s)} \right|_{\hat{\Phi}(s)=0} \quad (58)$$

As it can be observed in Fig. 23, the measurement of the audio susceptibility from the input port V_1 to the output port V_O matches with the calculated transfer function where the system dynamic behavior is modelled as two separate converters. From this measurement, it can be concluded that the converter output voltage V_O is not directly affected by perturbations on the converter input port V_1 or the duty cycle, but by the effect of these on the converter bidirectional port voltage V_2 . Therefore, as discussed in the converter modelling section, from a control point of view the proposed TPC effectively behaves as two separate converters to regulate the two power flows.

The performance of the proposed energy management system and control loops is verified by different experimental measurements [39]. Fig. 24 and Fig. 25 show the input currents of both of the converter input ports, I_1 and I_2 , as well as the load current, I_O , and the output voltage V_O . The converter is operating at $V_1 = 50$ V, $V_2 = 100$ V and $V_O = 370$ V. Fig. 24 (a) to (e) shows the transition between different operating modes due to variations of the available power at the renewable energy port, while the load demand remains constant ($P_O = 250$ W). Depending on the available power at the renewable energy port, the converter operating mode changes between DI mode, DO mode and SISO V_1 as illustrated in Table II. As it can be observed from the transitions shown in Fig. 24, variations of the power at the renewable energy port does not affect the voltage regulation at the output port, since the duty cycle control variable does not have an effect on the output voltage regulation when the converter operates in completely demagnetized mode.

In the same way, the transitions between different operating modes due to variations of the output port load demand are tested. Fig. 25 (a) to (f) shows the transition between different operating modes due to variations of the output power, while the power at the renewable energy port remains constant ($P_1 = 250$ W). Depending on the load demand, the converter operating mode changes between SISO V_1 , DI mode and DO mode, as presented in Table III. As it can be observed from

TABLE II
POWER AT THE PORTS FOR TRANSITIONS BETWEEN OPERATING MODES UNDER CONSTANT OUTPUT LOAD

	SISO V_1	SISO V_2	DI	DO
P_1 (W)	250	0	125	375
P_2 (W)	0	250	125	-125
P_O (W)	250	250	250	250

TABLE III
POWER AT THE PORTS FOR TRANSITIONS BETWEEN OPERATING MODES UNDER CONSTANT POWER AT THE RENEWABLE ENERGY SOURCE

	SISO V_1	DI	DO
P_1 (W)	250	250	250
P_2 (W)	0	125	-125
P_O (W)	250	375	125

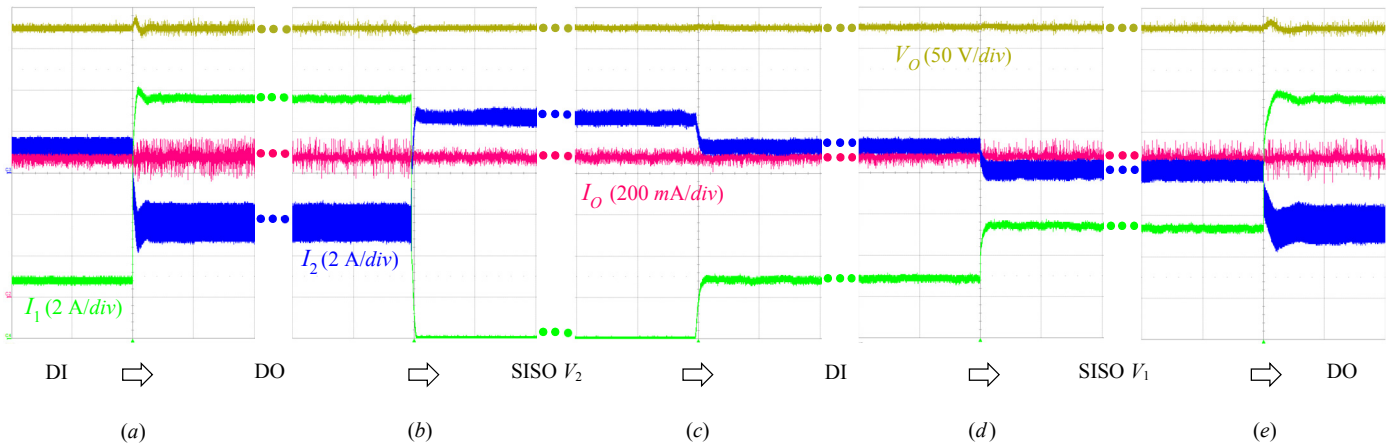


Fig. 24. Transition between different operating modes due to variations of the available power at the renewable energy port. Time scale: 20 ms/div.

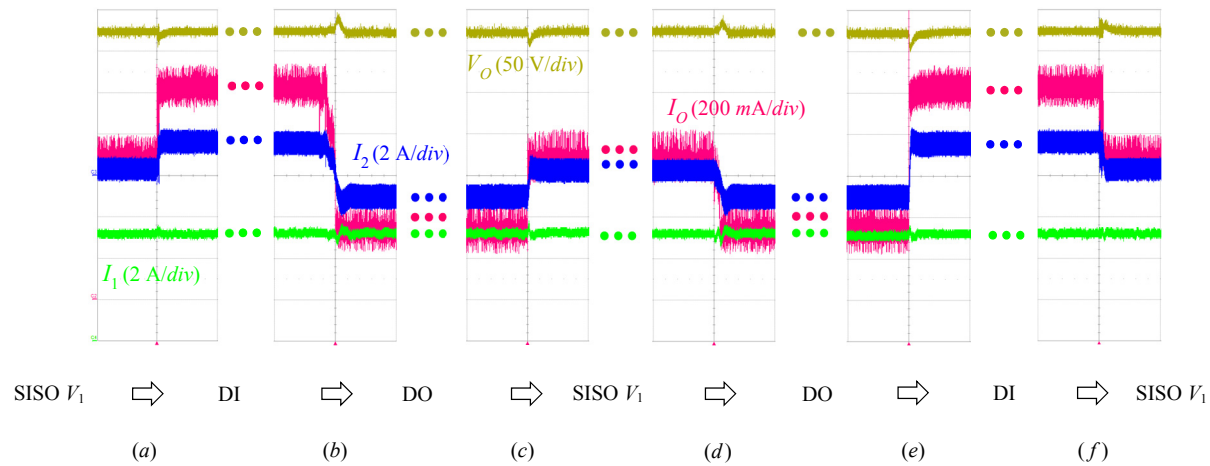


Fig. 25. Transition between different operating modes due to variations of the output port load demand. Time scale: 50 ms/div.

the different load steps in Fig. 25, variations of the output power do not affect the current at the renewable energy port, since the phase-shift control loop is decoupled from the duty cycle regulation that controls the power flow from the renewable energy source. Therefore, the power at the renewable energy port can be fully controlled, while the voltage at the output port is regulated, and the energy storage will compensate for the load dynamics. A disturbance in the output voltage V_O in Fig. 24 and in the input current I_1 in Fig. 25 can be observed due to the perturbation in the voltage V_2 at the bidirectional port under heavy load steps. The amplitude and dynamics of this perturbation are determined by the ability of the electronic load connected to the bidirectional port to regulate the voltage under CV operating mode.

VII. CONCLUSION

In this paper, an isolated soft-switched TPC to interface with hybrid renewable energy systems is presented. Its operating principle and design considerations are discussed and verified by simulation and experimental results. In order to control the power flow between the different ports, a duty cycle and phase-shift control scheme is adopted. The duty cycle is used to control the power flow between the two independent sources, whereas the phase-shift angle is employed to regulate the output voltage. The state-space modelling and control of the proposed TPC operating in completely demagnetized and fully magnetized mode is presented. The mathematical model is validated by simulation as well as experimental measurements of the plant and line-to-output transfer functions. The advantage of the proposed topology is that it can be dynamically modelled as individual converters, which makes it possible to design a control strategy with totally uncoupled control variables. This fact makes this topology a very interesting solution in renewable energy applications where an energy storage element is required, since full reutilization of the converter primary side switches is achieved, without having a negative impact in the controllability of the converter. By selecting the renewable source and the energy storage voltages, V_1 and V_2 , to require a duty cycle approximately to 0.5 the phase-shift value range

can be fully utilized. Experimental results demonstrate that the proposed energy/power management solution achieves effective control of the power flow among the input, bidirectional and output ports.

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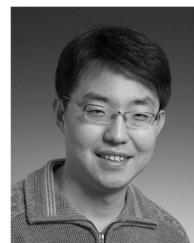
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